## Exercise 1.1

Subject: Separation operations in an ethanol process.
Given: Flow sheet for the process.
Find: Operation in each block of the process
Analysis: The flow sheet is as follows:


Starting from the left side of the top row, number the equipment blocks 1-5. On the next row, number them from right to left as 6-10.

1. The feed to the reactor contains ethylene, propylene, and water. The very incomplete reaction effluent of gas contains, in addition:ethyl alcohol, diethyl ether, acetaldehyde, and isopropyl alcohol.
2. Most of the chemicals, except most of the ethylene, are condensed and sent to item 4 . The remaining gas is sent to 3 .
3. The ethylene is recovered from the small quantity of other chemicals in the absorber. Most of the ethylene is recycled to 1 . The water and other chemicals are sent to 4 .
4. Remaining ethylene is flashed off and sent to 5 . The liquid contains most of the hydrocarbons and is sent to 6 .

## Exercise 1.1 (continued)

5. The small quantity of ethanol plus other chemicals is absorbed from the ethylene by water. The exit gas is vented. The liquid is wastewater that will have to be treated elsewhere.
6. The liquid from 4 is distilled to separate water from ethanol and other chemicals that are mostly diethyl ether and acetaldehyde. The bottoms is wastewater. The distillate is the organic chemicals that are sent to 7.
7. This unit is a fixed-bed catalytic reactor to convert acetaldehyde to ethanol. The reactor effluent is sent to 8 .
8. Diethyl ether and small amounts of the ethanol and other chemicals are removed as vapor by distillation and sent to 9 . The bottoms containing most of the ethanol is sent to 10 .
9. The diethyl ether in the vapor from 8 is recovered by absorbing the other chemicals with water, which is recycled to 4 .
10. The crude ethanol from 8 is distilled to obtain the near-azeotrope of ethanol and water. The bottoms is wastewater.

## Exercise 1.2

Subject: Mixing vs. separation
Given: Thermodynamic principles.
Find: Explanation for why mixing and separation are different.
Analysis: Mixing is a natural, spontaneous process. It may take time, but concentrations of components in a single fluid phase will tend to become uniform, with an increase in entropy. By the second law of thermodynamics, a natural process tends to randomness. The separation of a mixture does not occur naturally or spontaneously. Energy is required to separate the different molecular species.

## Exercise 1.3

Subject: Separation of a mixture requires a transfer of energy to it or the degradation of its energy.

Given: The first and second laws of thermodynamics.
Find: Explain why the separation of a mixture requires energy.
Analysis: As an example, consider the isothermal minimum (reversible) work of separation of an ideal binary gas mixture. Therefore, the change in enthalpy is zero. However, there is a change in entropy, determined as follows. From a chemical engineering thermodynamics textbook or Table 2.11, Eq. (4):

$$
\begin{aligned}
W_{\min } & =\sum_{\text {out }} n\left(h-T_{0} s\right)-\sum_{\text {in }} n\left(h-T_{0} s\right) \\
& =R T_{0}\left\{\sum_{\text {out }} n_{k} \sum y_{i, k} \ln \left(y_{i, k}\right)-\sum_{\text {in }} n_{j} \sum y_{i, j} \ln \left(y_{i, j}\right)\right\}
\end{aligned}
$$

It can be shown that regardless of values of y between 0 and 1 , that $W_{\min }$ is always positive. This minimum work is independent of the process.

## Exercise 1.4

Subject : Use of an ESA or an MSA to make a separations.
Given: Differences between an ESA and an MSA.
Find: State the advantages and disadvantages of ESA and MSA.
Analysis: With an MSA, an additional separator is needed to recover the MSA. Also, some MSA will be lost, necessitating the need for MSA makeup. If the MSA is incompletely recovered, a small amount of contamination may result. The use of an MSA can make possible a separation that cannot be carried out with an ESA. An ESA separation is easier to design.

## Exercise 1.5

Subject : Distillation versus liquid-liquid extraction..
Find: State differences between the two separation operations.

## Analysis:

1. Distillation involves both liquid and vapor phases. Extraction involves two liquid phases
2. Distillation uses an ESA. Extraction uses an MSA.
3. Distillation may occur over a wide range of temperature. Extraction usually occurs over a narrow range of temperature.
4. Mass transfer in distillation is relatively rapid. Mass transfer in extraction is relatively slow.
5. Distillation often uses more many stages. Extraction usually involves just several stages.
6. Distillation seldom requires mechanical agitation. Extraction is best carried out with mechanical agitation.
7. 

## Exercise 1.6

Subject: Osmotic pressure for the separation of water from sea water by reverse osmosis with a membrane.

Given: Sea water containing 0.035 g of salt/ $\mathrm{cm}^{3}$ of sea water on one side of a membrane Molecular weight of the salt $=31.5$
Temperature $=298 \mathrm{~K}$
Pure water on the other side of a membrane
Find: Minimum required pressure difference in kPa across the membrane
Analysis: The minimum pressure difference across the membrane is equal to the osmotic pressure of the sea water, since the osmotic pressure of pure water on the other side is zero. The equation given for osmotic pressure is $\pi=R T c / M$.

$$
\begin{aligned}
& R=8.314 \mathrm{kPa}-\mathrm{m}^{3} / \mathrm{kmol}-\mathrm{K} \\
& T=298 \mathrm{~K} \\
& c=0.035 \mathrm{~g} / \mathrm{cm}^{3}=35 \mathrm{~kg} / \mathrm{m}^{3} \\
& M=31.5 \mathrm{~kg} / \mathrm{kmol}
\end{aligned}
$$

Minimum pressure difference across a membrane $=$

$$
\pi=\frac{(8.314)(298)(35)}{31.5}=2,750 \mathrm{kPa}
$$

## Exercise 1.7

Subject: Basic separation techniques.
Given: A list of 10 separation operations.
Find: The basic separation technique for each of the 10 .

## Analysis:

1. Phase creation: distillation, flash vaporization
2. Phase addition: absorption, adsorption, extraction, stripping
3. Barrier: dialysis, gas permeation, pervaporation, reverse osmosis

## Exercise 1.8

Subject: Methods for removing organic pollutants from wastewater.
Given: Available industrial processes:
(1) adsorption
(2) distillation
(3) liquid-liquid extraction
(4) membrane separation
(5) stripping with air
(6) stripping with steam

Find: Advantages and disadvantages of each process.

## Analysis:

Some advantages and disadvantages are given in the following table:

| Method | Advantages | Disadvantages |
| :--- | :--- | :--- |
| Adsorption | Adsorbents are available. | Difficult to recover pollutant. <br> Best to incinerate it. |
| Distillation | May be practical if pollutant is <br> more volatile. | Impractical is water is more <br> volatile. |
| L-L extraction | Solvent are available. | Water will be contaminated with <br> solvent. |
| Membrane | May be practical if a membrane <br> can be found that is highly <br> selective for pollutant. | May need a large membrane area <br> if water is the permeate. |
| Air stripping | May be practical if pollutant is <br> more volatile. | Danger of producing a flammable <br> gas mixture. |
| Steam stripping | May be practical if pollutant is <br> more volatile. | Must be able to selectively <br> condense pollutant from <br> overhead. |

With adsorption, can incinerate pollutant, but with a loss of adsorbent.
With distillation, may be able to obtain a pollutant product.
With L-L extraction, will have to separate pollutant from solvent.
With a membrane, may be able to obtain a pollutant product.
With air stripping, may be able to incinerate pollutant.
With steam stripping may be able to obtain a pollutant product.

## Exercise 1.9

Subject: Removal of VOCs from a waste gas stream.
Given: Waste gas containing VOCs that must be removed by any of the following methods:
(1) absorption
(2) adsorption
(3) condensation
(4) freezing
(5) membrane separation

Find: Advantages and disadvantages of each method.

## Analysis:

Some advantages and disadvantages are given in the following table:

| Method | Advantages | Disadvantages |
| :--- | :--- | :--- |
| Absorption | Good absorbents probably exist. | Absorbent may stripped into the <br> waste gas. |
| Adsorption | Good adsorbents probably exist. | May have to incinerate the spent <br> adsorbent. |
| Condensation | May be able to recover the VOC <br> as a product. | May require high pressure and/or <br> low temperature. |
| Freezing | May be able to recover the VOC <br> as a product. | May require a low temperature. |
| Membrane | May be able to recover the VOC <br> as a product. | May be difficult to obtain high <br> selectivity. May require a very <br> high pressure. |

With absorption, may be able to distil the VOC from the absorbent.
With adsorption, may be able to incinerate the VOC or recover it.
With condensation, can recover the VOC as a product.
With freezing, can recover the VOC as a product.
With a membrane, can recover the VOC as a product.

The process shown on the following page shows a process for recovering acetone from air. In the first step, the acetone is absorbed with water. Although water is far from being the most ideal solvent because of the high volatility of acetone in water, the air will not be contaminated with an organic solvent. The acetone-water mixture is then easily separated by distillation, with recycle of the water.

## Exercise 1.9 (continued)

One possible process-flow diagram:


## Exercise 1.10

Subject: Separation of air into nitrogen and oxygen.
Given: Air to be separated.
Find: Three methods for achieving the separation.
Analysis: Three methods are used commercially for separating air into oxygen and nitrogen:

1. Gas permeation mainly for low capacities
2. Pressure-swing gas adsorption for moderate capacities.
3. Low-temperature distillation for high capacities.

## Exercise 1.11

Subject: Sequence of three distillation columns in Fig. 1.10 for separating light hydrocarbons.

Given: Feed to column C3 is stream 5 in Table 1.5. Alter the separation to produce a distillate containing $95 \mathrm{~mol} \% \mathrm{iC}_{4}$ at a recovery of $96 \%$.

Find: (a) Component flow rates in the distillate and bottoms from column C3.
(b) Percent purity of $\mathrm{nC}_{4}$ in the bottoms.
(c) Percent recovery of $\mathrm{iC}_{4}$, for $95 \mathrm{~mol} \% \mathrm{iC}_{4}$ in the distillate, that will maximize the percent purity of $\mathrm{nC}_{4}$ in the bottoms.

Assumptions: Because of the relatively sharp separation in column C 3 between $\mathrm{iC}_{4}$ and $\mathrm{nC}_{4}$, assume that all propane in the feed appears in the distillate and all $\mathrm{C}_{5} \mathrm{~S}$ appear in the bottoms.

Analysis: (a) Isobutane to the distillate $=(0.96)(171.1)=164.3 \mathrm{lbmol} / \mathrm{h}$
Total distillate rate $=164.3 / 0.95=172.9 \mathrm{lbmol} / \mathrm{h}$
Normal butane to the distillate $=172.9-2.2-164.3=6.4$
Material balance around column $\mathbf{C 3}$, in lbmol/h:
Component
Feed
Distillate
Bottoms

| Propane | 2.2 | 2.2 | 0.0 |
| :---: | ---: | ---: | ---: |
| Isobutane | 171.1 | 164.3 | 6.8 |
| Normal butane | 226.6 | 6.4 | 220.2 |
| Isopentane | 28.1 | 0.0 | 28.1 |
| Normal pentane | $\underline{17.5}$ | $\underline{0.0}$ | $\underline{17.5}$ |
| Total | 445.5 |  | 272.6 |

(b) $\%$ Purity of $\mathrm{nC}_{4}$ in bottoms $=(220.2 / 272.6) \times 100 \%=80.8 \%$
(c) Let $x=1 \mathrm{bmol} / \mathrm{h}$ of $\mathrm{nC}_{4}$ in the distillate
$y=\mathrm{lbmol} / \mathrm{h}$ of $\mathrm{iC}_{4}$ in the distillate
$P=$ mole fraction purity of $\mathrm{nC}_{4}$ in the bottoms

$$
\begin{equation*}
P=\frac{226.6-x}{(171.1-y)+(226.6-x)+28.1+17.5}=\frac{226.6-x}{443.3-y-x} \tag{1}
\end{equation*}
$$

Fractional purity of $\mathrm{iC}_{4}$ in the distillate $=\frac{y}{2.2+y+x}=0.95$
Combining (1) and (2) to eliminate $x$, and optimization of $P$ with respect to $y$ gives: $P=0.828$ or $82.8 \mathrm{~mol} \% \mathrm{nC}_{4}$ in the bottoms, $\quad x=6.8 \mathrm{lbmol} / \mathrm{h}, \quad y=171.1 \mathrm{lbmol} / \mathrm{h}$ Therefore, $100 \%$ recovery of $\mathrm{iC}_{4}$ in the distillate maximizes the purity of $\mathrm{nC}_{4}$ in the bottoms.

## Exercise 1.12

Subject: Sequence of two distillation columns, C1-C2, for the separation of alcohols.
Given: $500 \mathrm{kmol} / \mathrm{h}$ feed of $40 \%$ methanol (M), 35\% ethanol (E), $15 \%$ isopropanol (IP), and $10 \%$ normal propanol (NP), all in $\mathrm{mol} \%$. Distillate from column C 1 is $98 \mathrm{~mol} \% \mathrm{M}$, with a $96 \%$ recovery. Distillate from column C2 is $92 \mathrm{~mol} \%$ E, with a recovery of $95 \%$ based on the feed to column C 1 .

Find: (a) Component flow rates in the feed, distillates and bottoms.
(b) $\mathrm{Mol} \%$ purity of combined IP and NP in the bottoms from column C2.
(c) Maximum achievable purity of E in the distillate from column C 2 for $95 \%$ recovery of E from the feed to column C 1 .
(d) Maximum recovery of E from the feed to column C 1 for a $92 \mathrm{~mol} \%$ purity of E in the distillate from column C 2 .

Assumptions: Because of the sharp separation in column C1, neglect the presence of propanols in the distillate from column C1. Neglect the presence of M in the bottoms from column C 2 . The distillate from C 2 does not contain normal propanol.

Analysis: (a) M in distillate from $\mathrm{C} 1=(0.96)(500)(0.40)=192 \mathrm{kmol} / \mathrm{h}$
Total distillate from C1 $=192 / 0.98=195.92 \mathrm{kmol} / \mathrm{h}$
E in distillate from $\mathrm{C} 1=195.92-192=3.92 \mathrm{kmol} / \mathrm{h}$
E in feed to $\mathrm{C} 2=(500)(0.35)-3.92=171.08 \mathrm{kmol} / \mathrm{h}$
M in feed to $\mathrm{C} 2=\mathrm{M}$ in distillate from $\mathrm{C} 2=(500)(0.40)-192=8 \mathrm{kmol} / \mathrm{h}$
E in distillate from $\mathrm{C} 2=(500)(0.35)(0.95)=166.25 \mathrm{kmol} / \mathrm{h}$
Total distillate from C2 $=166.25 / 0.92=180.71 \mathrm{kmol} / \mathrm{h}$ IP in distillate from $\mathrm{C} 2=180.71-166.25-8=6.46 \mathrm{kmol} / \mathrm{h}$

Block flow diagram:


## Exercise 1.12 (Continued)

Analysis: (a) continued
Material balance table (all flow rates in $\mathrm{kmol} / \mathrm{h}$ ):

| Component | Stream 1 | $\underline{2}$ | $\underline{3}$ | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| M | 200 | 192.00 | 8.00 | 8.00 | 0.00 |
| E | 175 | 3.92 | 171.08 | 166.25 | 4.83 |
| IP | 75 | 0.00 | 75.00 | 6.46 | 68.54 |
| NP | $\underline{50}$ | 0.00 | 50.00 | 0.00 | $\underline{50.00}$ |
| Total | 500 | 195.92 | 304.08 | 180.71 | 123.37 |

The assumption of negligible NP in stream 4 is questionable and should be corrected when designing the column.
(b) $\mathrm{Mol} \%$ purity of $(\mathrm{IP}+\mathrm{NP})$ in bottoms of $\mathrm{C} 2=(68.54+50.00) / 123.37$ or 96.08\%
(c) If the overall recovery of E in the distillate from C 2 is fixed at $95 \%$, the maximum purity of E in that distillate occurs when no propanols appear in that distillate. Then,

$$
\mathrm{mol} \% \text { purity of } \mathrm{E}=100 \% \times 166.25 /(166.25+8.0)=95.41 \%
$$

(d) The maximum recovery of E in the distillate from C 2 occurs when E does not appear in the bottoms from C2. Thus, that maximum is $100 \% \mathrm{x}(171.08 / 175)=97.76 \%$

## Exercise 1.13

Subject: Pervaporation for the partial separation of ethanol and benzene
Given: $8,000 \mathrm{~kg} / \mathrm{h}$ of $23 \mathrm{wt} \%$ ethanol and $77 \mathrm{wt} \%$ benzene. Polymer membrane is selective for ethanol. Permeate is $60 \mathrm{wt} \%$ ethanol. Retentate is $90 \mathrm{wt} \%$ benzene.

Find: (a) and (b) Component flow rates in feed, permeate, and retentate on a diagram.
(c) Method to further separate the permeate.

Analysis: (a) and (b) Let: $P=$ permeate flow rate
$R=$ retentate flow rate
Total material balance: $8,000=P+R$
Ethanol material balance: $8,000(0.23)=(0.60) P+(0.10) R$
Solving (1) and (2) simultaneously, $P=2,080 \mathrm{~kg} / \mathrm{h}$ and $R=5,920 \mathrm{~kg} / \mathrm{h}$
The resulting material balance and flow diagram is:

(c) Gas adsorption, gas permeation, or distillation to obtain ethanol and the azeotrope, which can be recycled.

## Exercise 1.14

Subject: Creation of a flow sheet and material balance for the separation of acetone from nitrogen.

Given: Feed compositions and column splits.
Find: Material balance
Assumptions: Nitrogen is not soluble in MIBK.

Analysis: A typical flow diagram for an absorber followed by distillation to separate the absorbent from the acetone is shown in Figure 6.16c. However, in this exercise, the absorbent is not recycled. In practice it would be.

The material balance in $\mathrm{kmol} / \mathrm{h}$ for the process is as follows where the stream numbers correspond to the following streams:
1 - gas feed to absorber
2 - absorbent feed to absorber
3 - gas leaving absorber
4 - liquid bottoms from absorber to distillation
5 - distillate from distillation
6 - bottoms from distillation

| Steam | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{1}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{6}$ |
| :--- | ---: | ---: | ---: | ---: | :---: | ---: |
| Nitrogen | 0 | 100 | 100 | 0 | 0 | 0 |
| MIBK | 500 | 10 | 0 | 490 | 17.3 | 472.7 |
| Acetone | 0 | 45 | 900 | 855 | 850.2 | 4.8 |
| Total | 500 | 155 | 1000 | 1345 | 867.5 | 477.5 |

## Exercise 1.15

Subject: Separation of hydrogen from light gases by gas permeation with hollow fibers.
Given: Feed gas of $42.4 \mathrm{kmol} / \mathrm{h}$ of $\mathrm{H}_{2}, 7.0 \mathrm{kmol} / \mathrm{h}$ of $\mathrm{CH}_{4}$, and $0.5 \mathrm{kmol} / \mathrm{h}$ of $\mathrm{N}_{2}$ at $40^{\circ} \mathrm{C}$ and 16.7 MPa . Retentate exits at 16.2 kPa and permeate exits at 4.56 kPa . Gas heat capacity ratio $=\gamma=1.4$.

Assumptions: Membrane is not permeable to nitrogen. Reversible gas expansion with no heat transfer between the retentate and permeate. Separation index is based on mole fractions.

Find: (a) Component flows in the retentate and permeate if the mole ratio of methane to hydrogen in the permeate is 0.0117 and the split fraction (recovery), SF, for hydrogen from the feed to the permeate is 0.6038 .
(b) Percent purity of hydrogen in the permeate..
(c) Process flow diagram with complete material balance

Analysis: (a) and (c)
Hydrogen in permeate $=(0.6038)(42.4)=25.6 \mathrm{kmol} / \mathrm{h}$
Hydrogen in retentate $=42.4-25.6=16.8 \mathrm{kmol} / \mathrm{h}$
Let: $x=\mathrm{kmol} / \mathrm{h}$ of methane in permeate
Solving, $x=0.0117(25.6)=0.3 \mathrm{kmol} / \mathrm{h}$
Methane in the retentate $=7.0-0.3=6.7 \mathrm{kmol} / \mathrm{h}$
The resulting material balance and flow diagram is:

(b) Percent purity of hydrogen in permeate $=100 \% \times 25.6 / 25.9=98.8 \%$

## Exercise 1.16

Subject: Natural gas is produced when injecting nitrogen into oil wells. The nitrogen is then recovered from the gas for recycle.

Given: $170,000 \mathrm{SCFH}\left(60^{\circ} \mathrm{F}\right.$ and 14.7 psia$)$ of gas containing, in $\mathrm{mol} \%, 18 \% \mathrm{~N}_{2}, 75 \%$ $\mathrm{CH}_{4}$, and $7 \% \mathrm{C}_{2} \mathrm{H}_{6}$ at $100{ }_{0} \mathrm{~F}$ and 800 psia . Recover the $\mathrm{N}_{2}$ by gas permeation followed by adsorption.
The membrane is selective for nitrogen. The adsorbent is selective for methane. The adsorber operates at $100^{\circ} \mathrm{F}$, and 275 psia during adsorption and 15 psia during regeneration. Permeate exits the membrane unit at $20^{\circ} \mathrm{F}$ and a low pressure. Two stages of compression with cooling are needed to deliver the permeate gas to the adsorber. The regenerated gas from the adsorber is compressed in three stages with cooling, and is combined with the retentate to give the natural gas product.

Assumptions: The membrane is not permeable to ethane. The separation index, SP, defined by Eq. (1-4), is applied to the exiting retentate and permeate.

Find: (a) Draw a labeled process flow diagram.
(b) Compute the component material balance, based on the following data: Nitrogen in permeate $=90.83 \%$ of nitrogen in the feed. Mole ratio of methane to nitrogen in the permeate $=1.756$. The adsorption step gives $97 \mathrm{~mol} \%$ methane in the adsorbate with an $85 \%$ recovery based on the feed to the adsorber. The pressure drop across the membrane is 760 psi . The retentate exits at 800 psia .
The combined natural gas product contains $3 \mathrm{~mol} \%$ nitrogen. Place the results of the material balance in a table.

Analysis: (b) Refer to the process flow diagram on next page for stream numbers.
Let: ai = molar flow rate of $\mathrm{N}_{2}$ in $\mathrm{lbmol} / \mathrm{h}$ in stream i .
$\mathrm{bi}=$ molar flow rate of $\mathrm{CH}_{4}$ in $\mathrm{lbmol} / \mathrm{h}$ in stream i
$\mathrm{ci}=$ molar flow rate of ethane in $\mathrm{lbmol} / \mathrm{h}$ in stream i
Feed flow rate $=170,000$ SCFM $/ 379 \mathrm{SCF} / \mathrm{lbmol}$ at $\mathrm{SC}=448.5 \mathrm{lbmol} / \mathrm{h}$
$\mathrm{a} 1=0.18(448.5)=80.7, \quad \mathrm{~b} 1=0.75(448.5)=336.4, \quad \mathrm{c} 1=0.07(448.5)=31.4$
Because ethane does not permeate through the membrane, $\mathrm{c} 3=\mathrm{c} 6=31.4$ and $\mathrm{c} 2=\mathrm{c} 4=\mathrm{c} 5=0$
Solve for a 2 , $\mathrm{a} 3, \mathrm{a} 4, \mathrm{a} 5, \mathrm{a} 6$, and $\mathrm{b} 2, \mathrm{~b} 3, \mathrm{~b} 4, \mathrm{~b} 5$, b6 from 10 equations in 10 unknowns.
Nitrogen in permeate $=0.9083(80.7)=73.3$
For the permeate: $a 2 / b 2=1 / 732$
Component balances around the membrane unit:

$$
\mathrm{a} 2+\mathrm{a} 3=80.7 \quad \mathrm{~b} 2+\mathrm{b} 3=336.4
$$

Component balances around the adsorber:

$$
\mathrm{a} 2=\mathrm{a} 4+\mathrm{a} 5 \quad \mathrm{~b} 2=\mathrm{b} 4+\mathrm{b} 5
$$

## Exercise 1.16 (continued)

Component balances around the line mixer that mixes retentate with adsorbate gas:

$$
a 6=a 3+a 5
$$

$$
\mathrm{b} 6=\mathrm{b} 3+\mathrm{b} 5
$$

Methane purity in the adsorbate:

$$
\mathrm{b} 5=0.97(\mathrm{~b} 5+\mathrm{a} 5)
$$

Find: (b) (continued)
Methane recovery:

$$
\begin{aligned}
& \mathrm{b} 5=0.85 \mathrm{~b} 2 \\
& \mathrm{a} 6=0.03(\mathrm{a} 6+\mathrm{b} 6+31.4)
\end{aligned}
$$

All equations are linear. Solving these 10 equations with linear equation solver, such as in the Polymath program, results in the following material balance table:

| Component | Flow rate, $1 \mathrm{bmol} / \mathrm{h}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Stream 1 | $\underline{2}$ | 3 | 4 | 5 | $\underline{6}$ |
| Nitrogen | 80.7 | 73.3 | 7.4 | 69.9 | 3.4 | 10.8 |
| Methane | 336.4 | 128.7 | 207.7 | 19.3 | 109.4 | 317.1 |
| Ethane | 31.4 | 0.0 | 31.4 | 0.0 | 0.0 | 31.4 |
| Total | 448.5 | 202.0 | 246.5 | 89.2 | 112.8 | 359.3 |

(a) Labeled process flow diagram


The SP in the membrane block refers to a separation power $=\mathrm{a} 2 \mathrm{~b} 3 / \mathrm{a} 3 \mathrm{~b} 2$ computed from the material balance.

## Exercise 1.17

Subject: Partial condensation of a reactor effluent.
Given: The effluent from the partial condensation of the reactor effluent of a toluene hydrodealkylation process is cooledand partially condensed. The resulting liquid phase is distilled in a sequence of three distillation columns to give the following four products.

| Component | Off-gas, <br> $\mathbf{k m o l} / \mathbf{h}$ | Benzene <br> Product, <br> $\mathbf{k m o l} / \mathbf{h}$ | Toluene <br> Recycle, <br> $\mathbf{k m o l / h}$ | Biphenyl <br> Byproduct, <br> $\mathbf{k m o l} / \mathbf{h}$ |
| ---: | ---: | ---: | ---: | ---: |
| Hydrogen | 1.48 | 0.00 | 0.00 | 0.00 |
| Methane | 11.07 | 0.06 | 0.00 | 0.00 |
| Benzene | 0.80 | 264.72 | 1.33 | 0.00 |
| Toluene | 0.00 | 0.09 | 88.79 | 0.45 |
| Biphenyl | 0.00 | 0.00 | 0.02 | 4.59 |
| Total | 13.35 | 264.87 | 90.14 | 5.04 |

Assumptions: Continuous, steady-state operation.

## Find:

(a) The $\%$ recoveries for benzene and biphenyl.
(b) The $\mathrm{mol} \%$ purities for benzene and biphenyl.
(c) Why is there a toluene recycle stream?
(d) What would happen if the biphenyl was not separated from the toluene, but was recycled back to the reactor with the toluene?

## Analysis:

(a) Percent recovery of benzene $=264.72 /(264.72+0.80+1.33)=0.992$ or $99.2 \%$

Perceent recovery of biphenyl $=4.59 /(4.59+0.02)=0.9957$ or $99.57 \%$
(b) $\mathrm{Mol} \%$ purity of benzene in the benzene product $=264.72 / 264.87=0.9994$ or 99.94\%
$\mathrm{Mol} \%$ purity of biphenyl in the biphenyl product $=4.59 / 5.04=0.9107=91.07 \%$
(c) The reaction must be quite incomplete.
(d) The biphenyl would build up until the side reaction reached equilibrium.

## Exercise 1.18

## Subject: Separation by Gas Permeation

Given: A hydrodealkylation process of the type stated in Exercises 1.17 and 1.22, in which a gas rich in hydrogen and methane is separated from the reactor effluent by partial condensation. The gas is then sent to a gas permeation membrane separator (Operation 3 in table 1.3) to separate the hydrogen from the methane. The hydrogen is recycled to the reactor and the methane is used for fuel. The component flow rates for the membrane feed, membrane retentate, and recycled membrane permeate are as follows:

| Component | Feed, kmol/h | Retentate, kmol/h | Permeate, $\mathbf{k m o l} / \mathbf{h}$ |
| :--- | :--- | :--- | :--- |
| Hydrogen | 1575.7 | 157.6 | 1418.1 |
| Methane | 2388.1 | 2313.5 | 74.6 |
| Benzene | 29.8 | 29.8 | 0.0 |
| Toluene | 3.5 | 3.5 | 0.0 |
| Biphenyl | 0.0 | 0.0 | 0.0 |
| Total | 3997.1 | 2504.4 | 1492.7 |

Assumptions: Continuous, steady-state operation.

## Find:

(a) Percent recovery of hydrogen in permeate; methane in retentate. $\mathrm{Mol} \%$ purity of hydrogen in permeate and methane in retentate.
(b) Could hydrogen be separated from methane by distillation or absorption.

## Analysis:

(a) Percent recovery of hydrogen in permeate $=1418.1 / 1575.7=0.900$ or $90.0 \%$

Percent recovery of methane in retentate $=2313.5 / 2388.1=0.969$ or $96.9 \%$
$\mathrm{Mol} \%$ purity of hydrogen in permeate $=1418.1 / 1492.7=0.950$ or $95.0 \%$
$\mathrm{Mol} \%$ purity of methane in retentate $=2323.5 / 2504.4=0.928$ or $92.8 \%$
(b) They could be separated by distillation or absorption with a hydrocarbon absorbent such as propane. Both would probably require low temperature and high pressure. Therefore they may be expensive.

## Exercise 1.19

Subject: Suitable distillation sequence and all alternative distillation sequences
Given: The following feed to a distillation sequence:

| Component | Feed rate, <br> kmol/h | Normal <br> boiling <br> point, K |
| :--- | :--- | :--- |
| Methane | 19 | 112 |
| Benzene | 263 | 353 |
| Toluene | 85 | 384 |
| Ethylbenzene | 23 | 409 |

Assumptions: Applicability of distillation heuristics in Section 1.8.2.
Find: (a) A suitable distillation sequence of 3 columns. (b) All possible sequences of 4 columns for the separation of a 5-component feed.

Analysis: (a) The feed components are already ordered by volatility. The most applicable heuristic of Section 1.8.2 is: Remove, early in the sequence, those components of greatest molar percentage in the feed. This is because the amount of benzene in the feed greatly exceeds that of the other three components. Applying this heuristic to the first column, separate between benzene and toluene. Then, in the remaining two columns in parallel, separate the two resulting binary mixtures. Thus, a reasonable sequence is:


## Exercise 1.19 Continued

The above sequence can also be written in the following shorthand notation using the first letter of the name of each component:

$$
\mathrm{MBTE} \longrightarrow \mathrm{MT} / \mathrm{BE} \longrightarrow \mathrm{M} / \mathrm{T} \longrightarrow \mathrm{~B} / \mathrm{E}
$$

(b) For 5 products, A, B, C, D, and E, 4 distillation columns are needed and 14 alternative sequences are possible, as follow using shorthand notation:


## Exercise 1.20

Subject: Separation by distillation of an aqueous solution of bioproducts
Given: The following clarified fermentation broth feed at $37^{\circ} \mathrm{C}$ and 1 atm :

| Component | Conc., g/L water | Normal B.Pt., ${ }^{\mathbf{}} \mathbf{C}$ | Min. Product <br> Purity |
| :--- | :---: | :---: | :---: |
| Acetone | 9.9 | 56.5 | $90 \%$ |
| Ethanol | 19.8 | 78.4 | $90 \%$ |
| Water | 1000 | 100 | - |
| n-Butanol | 3.3 | 117 | $99.5 \%$ |

Assumptions: Ideal solutions (actually a poor assumption).
Find: A suitable distillation sequence using the heuristics of Section 1.7.
Analysis: Based on data in the above table, water is in the largest amount and should be removed early in the sequence. n-butanol is the highest purity and should be removed last in the sequence. Applying the heuristics of Section 1.8.2, separate between ethanol and water in the first column. Then separate the two binary mixtures, acetone-ethanol and water-butanol.

## Exercise 1.21

Subject: Separation of a mixture by a sequence of distillation columns.
Given: Feed stream containing in $\mathrm{kmol} / \mathrm{h}: 45.4 \mathrm{C} 3,136.1 \mathrm{iC} 4,226.8 \mathrm{nC} 4,181.4 \mathrm{iC} 5$, and 317.4 nC 5 . Three columns in series, $\mathrm{C} 1, \mathrm{C} 2$, and C3. Distillate from C1 is C3-rich with a $98 \%$ recovery. Distillate from C2 is iC4-rich with a $98 \%$ recovery. Distillate from C3 is nC4-rich with a $98 \%$ recovery. Bottoms from C3 is C5s-rich with a $98 \%$ recovery.

Find: (a) Process-flow diagram like Figure 1.10.
(b) Material-balance table like Table 1.5.
(c) Mole \% purities in a table like Table 1.6

Assumptions: Reasonable values for splits of iC4 to streams where they are not the main component.

## Analysis:

(a) Process-flow diagram:


## Exercise 1.21 (continued)

(b) Using given recoveries:

Propane in Stream $2=0.98(45.4)=44.5 \mathrm{kmol} / \mathrm{h}$
i-Butane in Stream $4=0.98(136.1)=133.4 \mathrm{kmol} / \mathrm{h}$
n-Butane in Stream $6=0.98(226.8)=222.3 \mathrm{kmol} / \mathrm{h}$
C5s in Stream $7=0.98(181.4+317.5)=488.9 \mathrm{kmol} / \mathrm{h}$
Material-balance table in $\mathrm{kmol} / \mathrm{h}$ :

| Comp | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| C 3 | 45.4 | 44.5 | 0.9 | 0.9 | 0.0 | 0.0 | 0.0 |
| iC 4 | 136.1 | 1.3 | 134.8 | 133.4 | 1.4 | 1.4 | 0.0 |
| nC 4 | 226.8 | 0.5 | 226.3 | 2.5 | 223.8 | 222.3 | 1.5 |
| $\mathrm{iC5}$ | 181.4 | 0.0 | 181.4 | 0.0 | 181.4 | 7.0 | 174.4 |
| nC5 | 317.5 | 0.0 | 317.5 | 0.0 | 317.5 | 3.0 | 314.5 |
| Total | 907.2 | 46.3 | 860.9 | 136.8 | 724.1 | 233.7 | 490.4 |

(c) $\quad \mathrm{Mol} \%$ purity of propane-rich product $=45.4 / 46.3=0.961=96.1 \%$
$\mathrm{Mol} \%$ purity of i-butane-rich product $=133.4 / 136.8=0.975=97.5 \%$
$\mathrm{Mol} \%$ purity of n -butane-rich product $=222.3 / 233.7=0.951=95.1 \%$
$\mathrm{Mol} \%$ purity of C 5 s -rich product $=(174.4+314.5) / 490.4=0.997=99.7 \%$

## Exercise 1.22

Subject: Distillation sequence for a wide-boiling mixture.
Given: The effluent from the reactor of a toluene hydrodealkylation process at $1265^{\circ} \mathrm{F}$ and 500 psia of the type stated in Exercise 1.17 is as follows:

| Component | Boiling Point, ${ }^{\mathbf{0} \mathbf{C}}$ | Flow Rate, kmol/h |
| :--- | ---: | ---: |
| Hydrogen (A) | -252.8 | 1577.1 |
| Methane (B) | -169.0 | 2399.2 |
| Benzene (C) | 80.1 | 296.6 |
| Toluene (D) | 110.6 | 92.8 |
| Biphenyl (E) | 255.2 | 4.6 |
| Total |  |  |

Assumptions: The applicability of heuristics in Section 1.8.2.
Find: Use the heuristics to separate the effluent into four products: (a) a gaseous mixture rich in hydrogen and methane; (b) a benzene-rich product of high purity; (c) a toluenerich mixture of low purity that is recycled to the reactor; and (c) a biphenyl byproduct of high purity. Use the heuristics to determine one or two favorable sequences. A sequence can contain one single-stage partial condenser in place of one multistage distillation column.

## Analysis:

Heuristic 1 might be interpreted to be applicable to components that are very flammable and explosive, as is the case for hydrogen and methane. This heuristic and number 3 favor separation of hydrogen and methane in the first separator, which can be a flash ( $\mathrm{AB} / \mathrm{CDE}$ ). The most difficult separation is between benzene and toluene, whose flow rates are much larger than biphenyl. Apply heuristics 3 and 4 (CD/E). Then separate benzene and toluene (C/D). A favorable sequence is: $\mathrm{AB} / \mathrm{CDE}, \mathrm{CD} / \mathrm{E}, \mathrm{C} / \mathrm{D}$.
Because of the small amount of biphenyl and the need for a high biphenyl purity, another favorable sequence is: $\mathrm{AB} / \mathrm{CDE}, \mathrm{C} / \mathrm{DE}, \mathrm{D} / \mathrm{E}$.

## Exercise 1.23

Subject: Distillation sequence for an alcohol mixture.
Given: A mixture of five alcohols to be separated into nearly pure products in a distillation sequence:

| Alcohol | Feed flow <br> rate, <br> kmol/h | Volatility relative <br> to 1-Hexanol |
| :--- | ---: | ---: |
| 1-Butanol (A) | 360 | 3.6 |
| 2-Methyl-1-Butanol (B) | 180 | 2.5 |
| 3-Methyl-2-Butanol (C) | 360 | 2.3 |
| 1-Pentanol (D) | 2520 | 1.8 |
| 1-Hexanol (E) | 3600 | 1.0 |
| Total | 7020 |  |

Assumptions: Applicability of the heuristics of Section 1.8.2.
Find: One or two feasible sequences.
Analysis: Heuristic 1 does not apply. Heuristic 3. suggests E be removed first since there is a good volatility difference between E and D and E has the highest flow rate ( $\mathrm{ABCD} / \mathrm{E}$ ). Using the same heuristic and reasoning, D is removed as bottoms in the second column (ABC/D). According to heuristic 4. since the volatility difference between $A$ and $B$ is greater than that between $B$ and $C$, remove $A(A / B C)$. Then separate $B$ from $C$ The column sequence : $\mathrm{ABCD} / \mathrm{E}, \mathrm{ABC} / \mathrm{D}, \mathrm{A} / \mathrm{BC}, \mathrm{B} / \mathrm{C}$. No other sequence comes close to satisfying the heuristics.

